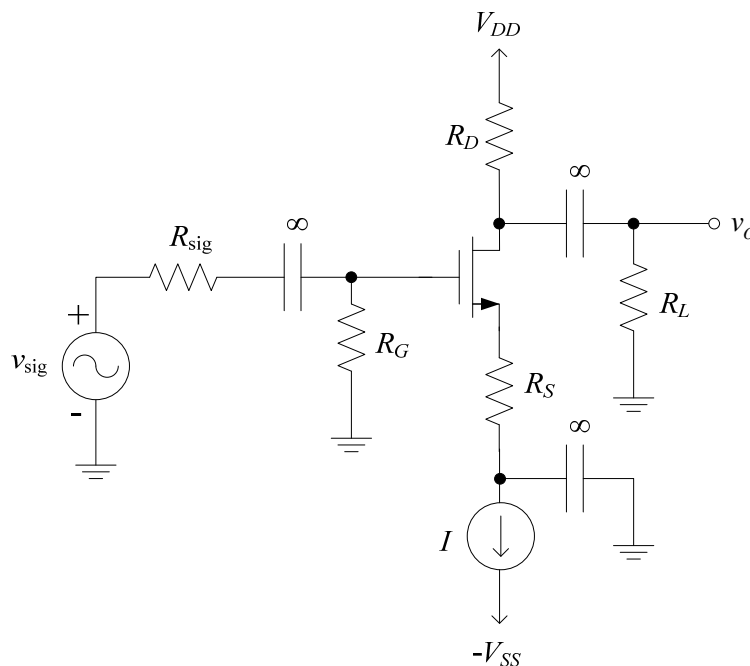


## Lecture 32: Common Source Amplifier with Source Degeneration.

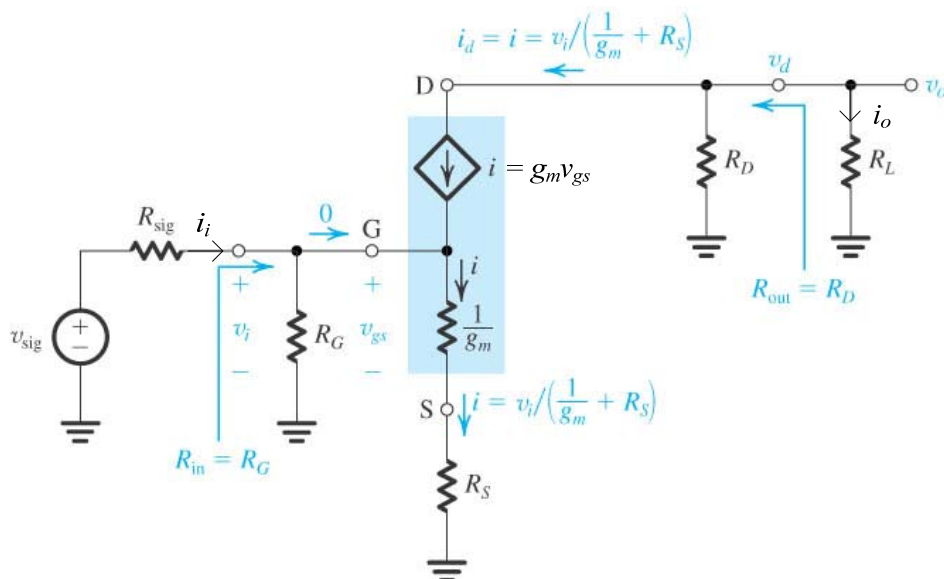
The small-signal amplification performance of the CS amplifier discussed in the previous lecture can be improved by including a series resistance in the source circuit. (This is very similar – if not identical – to the effect of adding emitter degeneration to the BJT CE amplifier.) This so-called **CS amplifier with source degeneration** circuit is shown in Fig. 4.44(a).



(Fig. 4.44a)

We have a choice of small-signal models to use for the MOSFET. A T model will simplify the analysis, on one hand, by allowing us to incorporate the effects of  $R_S$  by simply adding this value to  $1/g_m$  in the small-signal model, if we ignore  $r_o$ .

This small-signal circuit is shown in Fig. 4.44(b).



(Fig. 4.44b)

On the other hand, using the T model makes the analysis more difficult when  $r_o$  is included. (The hybrid  $\pi$  model is better at easily including the effects of  $r_o$ .) However,  $r_o$  in the MOSFET amplifier is large so we can **reasonably ignore** its effects for now in the expectation of making the analysis more tractable.

## Small-Signal Amplifier Characteristics

We'll now calculate the following small-signal quantities for this MOSFET common source amplifier with source degeneration:  $R_{in}$ ,  $A_v$ ,  $G_v$ ,  $G_i$ , and  $R_{out}$ .

- Input resistance,  $R_{in}$ . Referring to the small-signal equivalent circuit above in Fig. 4.44(b), with  $i_g = 0$ , then

$$R_{in} = R_G \quad (4.84),(1)$$

- Partial small-signal voltage gain,  $A_v$ . We see at the output side of the small-signal circuit in Fig. 4.44(b)

$$v_o = -g_m v_{gs} (R_D \parallel R_L) \quad (2)$$

which is the same result (ignoring  $r_o$ ) as we found for the CS amplifier without source generation. At the gate, however, we find through voltage division that

$$v_{gs} = \frac{1/g_m}{1/g_m + R_S} v_i = \frac{v_i}{1 + g_m R_S} \quad (4.86),(3)$$

This is a different result than for the CS amplifier in that  $v_{gs}$  is only a fraction of  $v_i$  here, whereas  $v_{gs} = v_i$  without  $R_S$ .

Substituting (3) into (2), gives the **partial** small-signal AC voltage gain to be

$$A_v \equiv \frac{v_o}{v_i} = \frac{-g_m (R_D \parallel R_L)}{1 + g_m R_S} \quad (4.88),(4)$$

- Overall small-signal voltage gain,  $G_v$ . As we did in the previous lecture, we can **derive an expression for  $G_v$  in terms of  $A_v$** . By definition,

$$G_v \equiv \frac{v_o}{v_{sig}} = \frac{v_i}{v_{sig}} \underbrace{\frac{v_o}{v_i}}_{=A_v} = \frac{v_i}{v_{sig}} A_v \quad (5)$$

Applying voltage division at the input of the small-signal equivalent circuit in Fig. 4.44(b),

$$v_i = \frac{R_{in}}{R_{in} + R_{sig}} v_{sig} \stackrel{(1)}{=} \frac{R_G}{R_G + R_{sig}} v_{sig} \quad (6)$$

Substituting (6) into (5) we the overall small-signal AC voltage gain for this CS amplifier with source degeneration to be

$$G_v = \frac{-R_G}{R_G + R_{sig}} \frac{g_m (R_D \parallel R_L)}{1 + g_m R_S} \quad (4.90), (7)$$

- Overall small-signal current gain,  $G_i$ . Using current division at the output in the small-signal model above in Fig. 4.44(b)

$$i_o = \frac{-R_D}{R_D + R_L} g_m v_{gs} \quad (8)$$

while at the input,

$$i_i = \frac{v_i}{R_G} \stackrel{(3)}{=} \frac{1 + g_m R_S}{R_G} v_{gs} \quad (9)$$

Substituting (9) into (8) we find that the overall small-signal AC current gain is

$$G_i \equiv \frac{i_o}{i_i} = \frac{-g_m R_D}{R_D + R_L} \frac{R_G}{1 + g_m R_S} \quad (10)$$

- Output resistance,  $R_{out}$ . From the small-signal circuit in Fig. 4.44(b) with  $v_{sig} = 0$  then  $i$  must be zero leading to

$$R_{out} = R_D \quad (11)$$

## Discussion

Adding  $R_S$  has a number of effects on the CS amplifier. (Notice, though, that it **doesn't affect the input and output resistances.**)

First, observe from (3)

$$v_{gs} = \frac{v_i}{1 + g_m R_S} \quad (3)$$

that we can employ  $R_S$  as a tool to lower  $v_{gs}$  relative to  $v_i$  and **lessen the effects of nonlinear distortion.**

This  $R_S$  also has the effect of **lowering the small-signal voltage gain**, which we can directly see from (7).

A major benefit, though, of using  $R_S$  is that the small-signal voltage (and current) gain can be made **much less dependent on the MOSFET device characteristics.** (We saw a similar effect in the CE BJT amplifier with emitter degeneration.)

We can see this here for the MOSFET CS amplifier using (7)

$$G_v = \frac{-R_G}{R_G + R_{sig}} \frac{g_m (R_D \parallel R_L)}{1 + g_m R_S} \quad (7)$$

The key factor in this expression is the second one. In the case that  $g_m R_S \gg 1$  then

$$G_v \approx \frac{-R_G}{R_G + R_{\text{sig}}} \frac{R_D \parallel R_L}{R_S} \quad (12)$$

which is **no longer dependent on  $g_m$** .

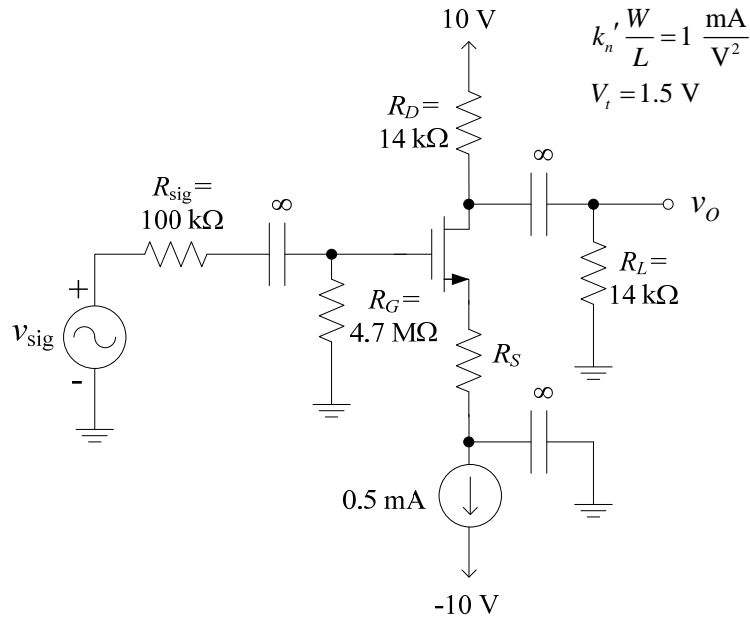
Conversely, without  $R_S$  in the circuit ( $R_S = 0$ ), we see from (7) that  $G_v \propto g_m$  and is directly dependent on the physical properties of the transistor (and the biasing) because

$$g_m \equiv \frac{i_d}{v_{gs}} = k_n' \frac{W}{L} (V_{GS} - V_t) \quad (4.61), (13)$$

in the case of an NMOS device.

The “**price**” we pay for this desirable behavior in (12) – where  $G_v$  is not dependent on  $g_m$  – is a reduced value for  $G_v$ . This  $G_v$  is largest when  $R_S = 0$ , as can be seen from (7).

**Example N32.1** (based on text exercises 4.32 and 4.33). Compute the small-signal voltage gain for the circuit below with  $R_S = 0$ ,  $k_n' W/L = 1 \text{ mA/V}^2$ , and  $V_t = 1.5 \text{ V}$ . For a 0.4-V<sub>pp</sub> sinusoidal input voltage, what is the amplitude of the output signal?



For the DC analysis, we see that  $V_G = 0$  and  $I_D = I_S = 0.5 \text{ mA}$ .  
(Why is  $V_G = 0$ ?) Consequently,

$$V_D = 10 - R_D I_D = 10 - 14\text{k} \cdot 0.5\text{m} = 3 \text{ V}$$

Assuming MOSFET operation in the saturation mode

$$I_D = \frac{1}{2} k_n' \frac{W}{L} (V_{GS} - V_t)^2$$

such that 
$$0.5 \text{ mA} = \frac{1}{2} 1 \times 10^{-3} (V_{GS} - 1.5)^2$$

or 
$$V_{GS} - 1.5 = \pm 1 \Rightarrow V_{GS} = 2.5 \text{ V or } 0.5 \text{ V}$$

Therefore, 
$$V_S = -2.5 \text{ V}$$

for operation in the saturation mode.

For the AC analysis, from (13)

$$g_m = 10^{-3} (2.5 - 1.5) = 1 \text{ mS}$$

Using this result in (7) with  $R_S = 0$  gives

$$G_v = \frac{-4.7\text{M}}{4.7\text{M} + 100\text{k}} 10^{-3} (14\text{k} \parallel 14\text{k}) = -6.85 \frac{\text{V}}{\text{V}}$$

For an input sinusoid with  $0.4\text{-}V_{\text{pp}}$  amplitude, then

$$V_o = G_v \cdot V_{\text{sig}} = 6.85 \cdot 0.4 \text{ V}_{\text{pp}} = 2.74 \text{ V}_{\text{pp}}$$

Will the MOSFET remain in the saturation mode for the entire cycle of this output voltage? For operation in the saturation mode,  $v_{DG} = v_D > V_t = 1.5 \text{ V}$ . On the negative swing of the output voltage,

$$v_D|_{\min} = V_D - \frac{v_{o,\text{pp}}}{2} = 3 - \frac{2.74}{2} = 1.63 \text{ V}$$

which is greater than  $V_t$ , so the MOSFET will not leave the saturation mode on the negative swings of the output voltage.

On the positive swings,

$$v_D|_{\max} = V_D + \frac{v_{o,\text{pp}}}{2} = 3 + \frac{2.74}{2} = 4.37 \text{ V}$$

which is less than  $V_{DD} = 10 \text{ V}$  so the MOSFET will not cutoff and leave the saturation mode.

(Interestingly, the MOSFET does leave the saturation mode on the negative swings for  $R_D = R_L = 15 \text{ k}\Omega$ , as used in the text exercises 4.32 and 4.33.)

Lastly, imagine that for some reason the input voltage is increased by a factor of 3 (to  $1.2 \text{ V}_{\text{pp}}$ ). What value of  $R_S$  can be used to keep the output voltage unchanged?



From (7), we can choose  $R_S$  so that the so-called **feedback factor**  $1 + g_m R_S$  equals 3. The output voltage amplitude will then be unchanged with this increased input voltage.

Hence, for

$$1 + g_m R_S = 3 \Rightarrow R_S = \frac{3-1}{g_m} = \frac{2}{10^{-3}} = 2 \text{ k}\Omega.$$

With  $R_S = 2 \text{ k}\Omega$  the new overall small-signal AC voltage gain is from (7)

$$G_v = \frac{-6.85}{1 + g_m R_S} = \frac{-6.85}{3} = -2.28 \frac{\text{V}}{\text{V}}$$

The overall small-signal voltage gain has gone down, but the amplitude of the output voltage has stayed the same since the input voltage amplitude was increased.